

# NAG Toolbox for MATLAB

## f08gu

### 1 Purpose

f08gu multiplies an arbitrary complex matrix  $C$  by the complex unitary matrix  $Q$  which was determined by f08gs when reducing a complex Hermitian matrix to tridiagonal form.

### 2 Syntax

```
[ap, c, info] = f08gu(side, uplo, trans, ap, tau, c, 'm', m, 'n', n)
```

### 3 Description

f08gu is intended to be used after a call to f08gs, which reduces a complex Hermitian matrix  $A$  to real symmetric tridiagonal form  $T$  by a unitary similarity transformation:  $A = QTQ^H$ . f08gs represents the unitary matrix  $Q$  as a product of elementary reflectors.

This function may be used to form one of the matrix products

$$QC, Q^H C, CQ \text{ or } CQ^H,$$

overwriting the result on  $C$  (which may be any complex rectangular matrix).

A common application of this function is to transform a matrix  $Z$  of eigenvectors of  $T$  to the matrix  $QZ$  of eigenvectors of  $A$ .

### 4 References

Golub G H and Van Loan C F 1996 *Matrix Computations* (3rd Edition) Johns Hopkins University Press, Baltimore

### 5 Parameters

#### 5.1 Compulsory Input Parameters

1: **side** – string

Indicates how  $Q$  or  $Q^H$  is to be applied to  $C$ .

**side** = 'L'

$Q$  or  $Q^H$  is applied to  $C$  from the left.

**side** = 'R'

$Q$  or  $Q^H$  is applied to  $C$  from the right.

*Constraint:* **side** = 'L' or 'R'.

2: **uplo** – string

This **must** be the same parameter **uplo** as supplied to f08gs.

*Constraint:* **uplo** = 'U' or 'L'.

3: **trans** – string

Indicates whether  $Q$  or  $Q^H$  is to be applied to  $C$ .

**trans** = 'N'

$Q$  is applied to  $C$ .

**trans** = 'C'

$Q^H$  is applied to  $C$ .

*Constraint:* **trans** = 'N' or 'C'.

4: **ap(\*) – complex array**

**Note:** the dimension of the array **ap** must be at least  $\max(1, m \times (m + 1)/2)$  if **side** = 'L' and at least  $\max(1, n \times (n + 1)/2)$  if **side** = 'R'.

Details of the vectors which define the elementary reflectors, as returned by f08gs.

5: **tau(\*) – complex array**

**Note:** the dimension of the array **tau** must be at least  $\max(1, m - 1)$  if **side** = 'L' and at least  $\max(1, n - 1)$  if **side** = 'R'.

Further details of the elementary reflectors, as returned by f08gs.

6: **c(ldc,\*) – complex array**

The first dimension of the array **c** must be at least  $\max(1, m)$

The second dimension of the array must be at least  $\max(1, n)$

The  $m$  by  $n$  matrix  $C$ .

## 5.2 Optional Input Parameters

1: **m – int32 scalar**

*Default:* The first dimension of the array **c**.

$m$ , the number of rows of the matrix  $C$ ;  $m$  is also the order of  $Q$  if **side** = 'L'.

*Constraint:*  $m \geq 0$ .

2: **n – int32 scalar**

*Default:* The second dimension of the array **c**.

$n$ , the number of columns of the matrix  $C$ ;  $n$  is also the order of  $Q$  if **side** = 'R'.

*Constraint:*  $n \geq 0$ .

## 5.3 Input Parameters Omitted from the MATLAB Interface

ldc, work

## 5.4 Output Parameters

1: **ap(\*) – complex array**

**Note:** the dimension of the array **ap** must be at least  $\max(1, m \times (m + 1)/2)$  if **side** = 'L' and at least  $\max(1, n \times (n + 1)/2)$  if **side** = 'R'.

Is used as internal workspace prior to being restored and hence is unchanged.

2: **c(ldc,\*) – complex array**

The first dimension of the array **c** must be at least  $\max(1, m)$

The second dimension of the array must be at least  $\max(1, n)$

**c** contains  $QC$  or  $Q^H C$  or  $CQ$  or  $CQ^H$  as specified by **side** and **trans**.

3: **info** – int32 scalar

**info** = 0 unless the function detects an error (see Section 6).

## 6 Error Indicators and Warnings

Errors or warnings detected by the function:

**info** =  $-i$

If **info** =  $-i$ , parameter  $i$  had an illegal value on entry. The parameters are numbered as follows:

1: **side**, 2: **uplo**, 3: **trans**, 4: **m**, 5: **n**, 6: **ap**, 7: **tau**, 8: **c**, 9: **ldc**, 10: **work**, 11: **info**.

It is possible that **info** refers to a parameter that is omitted from the MATLAB interface. This usually indicates that an error in one of the other input parameters has caused an incorrect value to be inferred.

## 7 Accuracy

The computed result differs from the exact result by a matrix  $E$  such that

$$\|E\|_2 = O(\epsilon)\|C\|_2,$$

where  $\epsilon$  is the *machine precision*.

## 8 Further Comments

The total number of real floating-point operations is approximately  $8m^2n$  if **side** = 'L' and  $8mn^2$  if **side** = 'R'.

The real analogue of this function is f08gg.

## 9 Example

```
side = 'Left';
uplo = 'L';
trans = 'No transpose';
ap = [complex(-2.28, +0);
      complex(-4.33845594653213, +0);
      complex(0.3278606760921924, -0.1251226092264437);
      complex(-0.1412565637506947, -0.366636483973957);
      complex(-0.1284569816493291, +0);
      complex(-2.022594578622617, +0);
      complex(-0.308321908008089, +0.1763226364726777);
      complex(-0.1665932537524081, +0);
      complex(-1.802322978338735, +0);
      complex(-1.924949764598263, +0)];
tau = [complex(1.410284216766754, +0.4679084045148932);
       complex(1.302420369434775, +0.7853320742529579);
       complex(1.093973715923082, -0.9955746786231597)];
c = [complex(0.7298945743917051, +0), complex(-0.2595449733877608, +0);
     complex(0.6258777805557931, +0), complex(-0.04325496258655371, +0);
     complex(0.2513449473644084, +0), complex(0.495247410182068, +0);
     complex(0.1111603864444915, +0), complex(0.8279465065502341, +0)];
[apOut, cOut, info] = f08gu(side, uplo, trans, ap, tau, c)

apOut =
    -2.2800
    -4.3385
     0.3279 - 0.1251i
```

```
-0.1413 - 0.3666i
-0.1285
-2.0226
-0.3083 + 0.1763i
-0.1666
-1.8023
-1.9249
cOut =
  0.7299          -0.2595
 -0.1663 - 0.2061i   0.5969 + 0.4214i
 -0.4165 - 0.1417i  -0.2965 - 0.1507i
  0.1743 + 0.4162i   0.3482 + 0.4085i
info =
      0
```

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